

Introduction to LiveLink™ *for* MATLAB®



Introduction to LiveLink™ for MATLAB®

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Version:

May 2012

COMSOL 4.3

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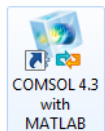
Introduction

This guide introduces you to LiveLink™ for MATLAB®. The examples guide you through the process of setting-up a COMSOL model and explain how to use COMSOL Multiphysics within the MATLAB scripting environment.

Starting COMSOL with MATLAB

STARTING ON WINDOWS

To start COMSOL Multiphysics with MATLAB double-click on the COMSOL with MATLAB icon available on the desktop.



This opens the MATLAB desktop together with the COMSOL server, which is represented by the command window appearing in the background.

STARTING ON MAC OS X

Navigate to **Applications>COMSOL 4.3>COMSOL 4.3 with MATLAB**.

An alternative way is to use a terminal window and enter the command:

```
comsol server matlab
```

STARTING ON LINUX

Start a terminal prompt and run the `comsol` command, which is located inside the bin folder in the COMSOL installation directory:

```
comsol server matlab
```

THE COMSOL CLIENT SERVER

The LiveLink interface is based on the COMSOL client/server architecture. A COMSOL thin client is running inside MATLAB and has access to the COMSOL API through the MATLAB Java interface. Model information is stored in a *model object* available on the COMSOL server. The thin client communicates with the COMSOL server, enabling you to generate, modify, and solve COMSOL model objects at the MATLAB prompt.

When starting **COMSOL with MATLAB**, you open both the COMSOL server and the MATLAB desktop. The first time you are required to enter a username and password. Once this information is entered, the client/server communication is established. The information is stored in the user preferences, so that subsequent starts do not require you to enter it again.

Both the COMSOL server and the MATLAB desktop are run on the same computer. For computations requiring more memory you can connect to a remote server, but this configuration requires a floating network license.

Note that the COMSOL Desktop is not used when running COMSOL Multiphysics with MATLAB. You can start the COMSOL Desktop separately to import models available in the COMSOL server connected to MATLAB. See “Exchanging Models with the COMSOL Desktop” for more information.

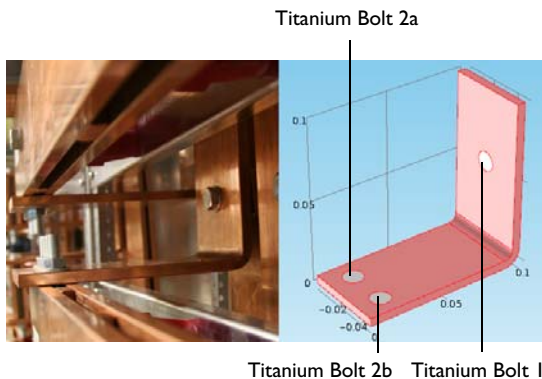
A Thorough Example: The Busbar

This example familiarizes you with the COMSOL model object and the COMSOL API syntax. In this section, learn how to:

- Create a geometry
- Set up a mesh and apply physics properties
- Solve the problem
- Generate results for analysis
- Exchange the model between the scripting interface of MATLAB and the COMSOL desktop.

The model you are building at the MATLAB command line is the same model described in the *Introduction to COMSOL Multiphysics*. The difference is that in that guide it is set up using the COMSOL Desktop instead of the COMSOL model object.

This multiphysics example describes electrical heating in a busbar. The busbar is used to conduct a direct current from a transformer to an electric device, which is made of copper with titanium bolts, as shown in the figure below.



ABOUT COMPACT NOTATION

This example uses *compact notation* to shorten the commands to be entered at the MATLAB command line. The compact notation uses MATLAB variables as links to provide direct access to COMSOL model object features.

For example, to create a block using the compact notation, enter:

```
blk1 = geom1.feature.create('blk1', 'Block');  
blk1.setIndex('size', '2', 0);  
blk1.setIndex('size', '3', 1);
```

This creates a block, then changes its width to 2 and its depth to 3.

Compared to above, the commands using a full notation are:

```
geom1.feature.create('blk1', 'Block');  
geom1.feature('blk1').setIndex('size', '2', 0);  
geom1.feature('blk1').setIndex('size', '3', 1);
```

When a model object is saved in the M-file format the full notation is always used.

Note: 'blk1' (with quotes) is the block geometry tag defined inside the COMSOL model object. The variable `blk1` (without quotes), defined only in MATLAB, is the link to the block feature. By linking MATLAB variables to features you can directly access and modify features of the COMSOL model object in an efficient manner:

ABOUT THE MODEL OBJECT

The model object contains all the information about a model, from the geometry to the results. The model object is defined on the COMSOL server and can be accessed at the MATLAB command line using a link in MATLAB.

- 1 Start COMSOL with MATLAB as in the section "Starting COMSOL with MATLAB".
- 2 Start modeling by creating a model object on the COMSOL server:

```
model = ModelUtil.create('Model');
```

The model object on the COMSOL server has the tag `Model` while the variable `model` is its link in MATLAB.

To access and modify the model object the LiveLink interface uses the COMSOL API syntax.

- 3 Set a name for the model object:

```
model.name('busbar');
```

The name defined by the `name` method is intended only for visualization purposes when exporting the model to the COMSOL Desktop.

ABOUT GLOBAL PARAMETERS

If you plan to solve your problem for several different parameter values, it is convenient to define them in the Parameters node, and to take advantage of the COMSOL parametric sweep functionality. Global parameters can be used in expressions during all stages of the model set-up, for example, when creating geometry, applying physics, or defining the mesh.

- 1 Define the parameters for the busbar model:

```
model.param.set('L', '9[cm]', 'Length of the busbar');
model.param.set('rad_1', '6[mm]', 'Radius of the fillet');
model.param.set('tbb', '5[mm]', 'Thickness');
model.param.set('wbb', '5[cm]', 'Width');
model.param.set('mh', '6[mm]', 'Maximum element size');
model.param.set('htc', '5[W/m^2/K]', 'Heat transfer coefficient');
model.param.set('Vtot', '20[mV]', 'Applied electric potential');
```

GEOMETRY

- 1 Create a 3D geometry node:

```
geom1 = model.geom.create('geom1', 3);
```

The create method of the geometry node requires as input a tag for the geometry name ('geom1'), and the geometry space dimension (3 for 3D).

- 2 The initial geometry is obtained by extruding a 2D drawing. Create a work plane tagged 'wp1', and set it as the xz-plane of the 3D geometry:

```
wp1 = geom1.feature.create('wp1', 'WorkPlane');
wp1.set('quickplane', 'xz');
```

- 3 In this work plane, create a rectangle and set the width to $L+2 \cdot t_{bb}$ and the height to 0.1:

```
r1 = wp1.geom.feature.create('r1', 'Rectangle');
r1.set('size', {'L+2*tbb' '0.1'});
```

Note: When the `size` properties of the rectangle are enclosed with single quotes ' ', it indicates that the variables `L` and `tbb` are defined within the model object. In this case they are defined in the Parameters node.

- 4 Create a second rectangle and set the width to $L+t_{bb}$ and the height to $0.1-t_{bb}$. Then change the rectangle position to $(0;t_{bb})$:

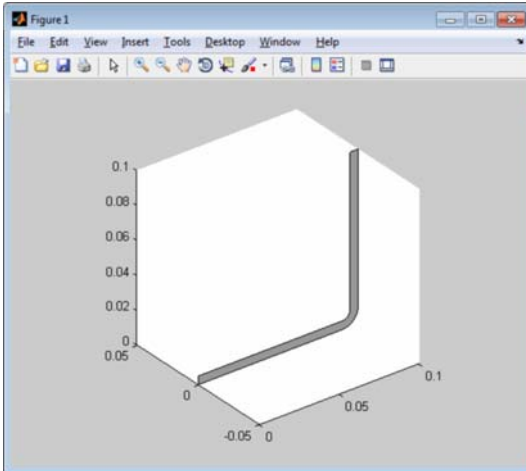
```
r2 = wp1.geom.feature.create('r2', 'Rectangle');
r2.set('size', {'L+tbb' '0.1-tbb'});
r2.set('pos', {'0' 'tbb'});
```

- 5 Subtract rectangle **r2** from rectangle **r1**, by creating a **Difference** feature with the 'input' property set to **r1** and the 'input2' property set to **r2**:

```
dif1 = wp1.geom.feature.create('dif1', 'Difference');  
dif1.selection('input').set({'r1'});  
dif1.selection('input2').set({'r2'});
```

Display the current geometry using **mphgeom**. Enter at the MATLAB prompt:

```
mphgeom(model, 'geom1');
```



- 6 Round the inner corner by creating a **Fillet** feature and set point 3 in the **selection** property. Then set the **radius** to **tbb**:

```
fil1 = wp1.geom.feature.create('fil1', 'Fillet');  
fil1.selection('point').set('dif1(1)', 3);  
fil1.set('radius', 'tbb');
```

- 7 Round the outer corner by creating a new **Fillet** feature, then select point 6 and set the **radius** to **2*tbb**:

```
fil2 = wp1.geom.feature.create('fil2', 'Fillet');  
fil2.selection('point').set('fil1(1)', 6);  
fil2.set('radius', '2*tbb');
```

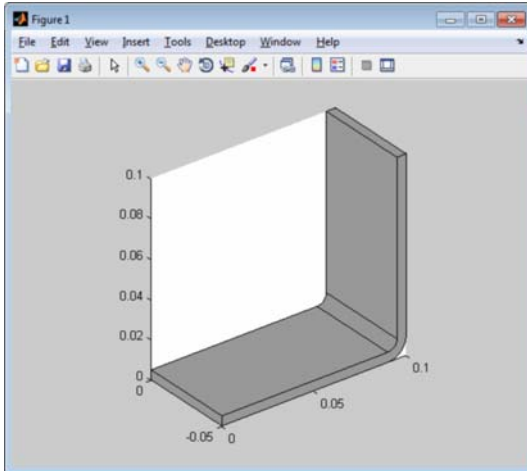
For geometry operations the name of the resulting geometry objects is formed by appending a numeral in parenthesis to the tag of the geometry operation. Above, 'fil1(1)' is the result of the 'fil1' operation.

- 8 Extrude the geometry objects in the work plane. Create an **Extrude** feature, set the work plane **wp1** as **input** and the **distance** to **wbb**:

```
ext1 = geom1.feature.create('ext1', 'Extrude');  
ext1.selection('input').set({'wp1'});  
ext1.set('distance', {'wbb'});
```

You can plot the current geometry by entering the following command at the MATLAB prompt:

```
mphgeom(model)
```



The busbar shape is now generated. Next create the cylinder that represent the bolts connecting the busbar to the external frame (not represented in the model).

- 9 Create a new work plane and set the **planetype** property to **faceparallel**. Then set the **selection** to boundary 8:

```
wp2 = geom1.feature.create('wp2', 'WorkPlane');  
wp2.set('planetype', 'faceparallel');  
wp2.selection('face').set('ext1(1)', 8);
```

- 10 Create a circle and set the radius to **rad_1**:

```
c1 = wp2.geom.feature.create('c1', 'Circle');  
c1.set('r', 'rad_1');
```

- 11 Create an **Extrude** node, select the second work plane **wp2** as **input**, and then set the extrusion distance to **-2*tbb**:

```
ext2 = geom1.feature.create('ext2', 'Extrude');  
ext2.selection('input').set({'wp2'});  
ext2.set('distance', {'-2*tbb'});
```

- 12 Create a new workplane, set **planetype** to **faceparallel**, then set the selection to boundary 4:

```
wp3 = geom1.feature.create('wp3', 'WorkPlane');  
wp3.set('planetype', 'faceparallel');  
wp3.selection('face').set('ext1(1)', 4);
```

- 13 Create a circle, then set the radius to **rad_1** and set the position of the center to **(-L/2+1.5e-2;-wbb/4)**:

```
c2 = wp3.geom.feature.create('c2', 'Circle');
c2.set('r', 'rad_1');
c2.set('pos', {'-L/2+1.5e-2' '-wbb/4'});
```

- 14 Create a second circle in the work plane by copying the previous circle and displacing it a distance $wbb/2$ in the y-direction:

```
copy1 = wp3.geom.feature.create('copy1', 'Copy');
copy1.selection('input').set({'c2'});
copy1.set('disply', 'wbb/2');
```

- 15 Extrude the circles **c2** and **copy1** from the work plane **wp3** a distance $-2*tbb$:

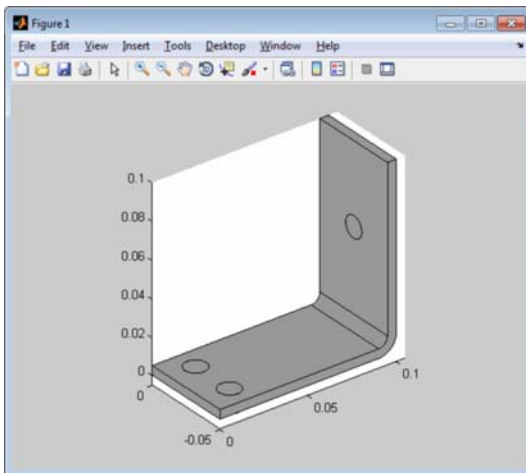
```
ext3 = geom1.feature.create('ext3', 'Extrude');
ext3.selection('input').set({'wp3.c2' 'wp3.copy1'});
ext3.set('distance', {'-2*tbb'});
```

- 16 Build the entire geometry sequence, including the finalize node using the **run** method:
- ```
geom1.run;
```

**Note:** The run method only builds features which need re-building or have not yet been built, including the finalize node.

- 17 Display the geometry with the **mphgeom** command:

```
mphgeom(model)
```



## SELECTIONS

---

You can create selections of geometric entities such as domains, boundaries, edges, or points. These selections can be accessed during the modeling process with the advantage of not having to select the same entities several times.

- 1 To create a domain selection corresponding to the titanium bolts, named **Ti bolts** enter:

```
sel1 = model.selection.create('sel1');
sel1.set([2 3 4 5 6 7]);
sel1.name('Ti bolts');
```

## MATERIAL PROPERTIES

---

The Material node of the model object stores the material properties. In this example the Joule Heating interface is used to involve both an electric current and a heat balance. Thus, the electrical conductivity, the heat capacity, the relative permittivity, the density, and the thermal conductivity of the materials all need to be defined.

The busbar is made of copper and the bolts are made of titanium. The properties you need for these two materials are listed in the table below:

| PROPERTY                | COPPER           | TITANIUM         |
|-------------------------|------------------|------------------|
| Electrical conductivity | 5.998e7 [S/m]    | 7.407e5 [S/m]    |
| Heat capacity           | 385 [J / (kg*K)] | 710 [J / (kg*K)] |
| Relative permittivity   | 1                | 1                |
| Density                 | 8700 [kg/m^3]    | 4940 [kg/m^3]    |
| Thermal conductivity    | 400 [W / (m*K)]  | 7.5 [W / (m*K)]  |

- 1 Create the first material, copper:  

```
mat1 = model.material.create('mat1');
```
- 2 Set the properties for the 'electricconductivity', 'heatcapacity', 'relpermittivity', 'density' and 'thermalconductivity' according to the table above:

```
mat1.materialModel('def').set('electricconductivity', {'5.998e7[S/m]'});
mat1.materialModel('def').set('heatcapacity', '385[J/(kg*K)]');
mat1.materialModel('def').set('relpermittivity', {'1'});
mat1.materialModel('def').set('density', '8700[kg/m^3]');
mat1.materialModel('def').set('thermalconductivity', {'400[W/(m*K)]'});
```

- 3 Set the name of the material to 'Copper'. By default the first material is assigned to all domains:

```
mat1.name('Copper');
```

- 4 Create a second material using the material properties for titanium, and set its name to 'Titanium' :

```
mat2 = model.material.create('mat2');
mat2.materialModel('def').set('electricconductivity', {'7.407e5[S/m]'});
mat2.materialModel('def').set('heatcapacity', '710[J/(kg*K)]');
mat2.materialModel('def').set('relpermittivity', {'1'});
mat2.materialModel('def').set('density', '4940[kg/m^3]');
mat2.materialModel('def').set('thermalconductivity', {'7.5[W/(m*K)]'});
mat2.name('Titanium');
```

- 5 Assign the material to the selection 'sel1' (corresponding to the bolt domains) created previously:

```
mat2.selection.named('sel1');
```

Only one material per domain can be assigned. This means that the last operation automatically removes the bolts from the selection of the copper material.

## PHYSICS INTERFACE

---

The Physics node contains the settings of the physics interfaces, including the domain and the boundary settings. Settings are grouped together according to the physics interface they belong to. To model the electrothermal interaction of this example, add the **JouleHeating** interface to the model. Apply a fixed electric potential to the upper bolt and ground the two lower bolts. In addition, assume that the device is cooled by convection, approximated by a heat flux with a defined heat transfer coefficient on all outer faces except where the bolts are connected.

- 1 Create the **JouleHeating** interface on the **geom1** geometry:  

```
jh = model.physics.create('jh', 'JouleHeating', 'geom1');
```
- 2 Create a heat flux boundary condition and set the type to **InwardHeatFlux**:  

```
hf1 = jh.feature.create('hf1', 'HeatFluxBoundary', 2);
```

**Note:** The third argument of the create method, the space dimension **sdim**, indicates at which geometry level (domain, boundary, edge, or point) the feature should be applied to. In the above commands 'HeatFluxBoundary' feature applies to boundaries, which have the space dimension 2.

- 3 Now apply the cooling to all exterior boundaries 1 to 43 except the bolt connection boundaries 8, 15, and 43. An **InwardHeatFlux** boundary condition requires a heat transfer coefficient. Set its value to the previously defined parameter **htc**:

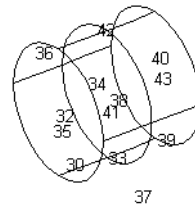
```
hf1.set('HeatFluxType', 'InwardHeatFlux');
hf1.selection.set([1:7 9:14 16:42]);
hf1.set('h', 'htc');
```

- 4 As you have noticed, defining selections requires you to know the entity indices. To view the boundary indices, display the geometry with the face labels:

```
mphgeom(model, 'geom1', 'facemode', 'off', 'facelabels', 'on')
```

You can use the controls in the window to zoom and pan to read off the indices.

**Note:** Alternative methods for obtaining entity indices are described in the *LiveLink for MATLAB User Guide*. These include the use of point coordinates, selection boxes, or adjacency information.



- 5 Create an electric potential boundary condition; set the selection to boundary 43; then set the electric potential to **Vtot**:

```
pot1 = jh.feature.create('pot1', 'ElectricPotential', 2);
pot1.selection.set([43]);
pot1.set('V0', 'Vtot');
```

- 6 Apply a ground boundary condition to boundaries 8 and 15:

```
gnd1 = jh.feature.create('gnd1', 'Ground', 2);
gnd1.selection.set([8 15]);
```

The model object includes default properties so you do not need to set properties for all boundaries. For example, the **Joule heating** physics interface uses a current insulation as default boundary condition for the current balance.

## MESH

---

The mesh sequence is stored in the Mesh node. Several mesh sequences, also called mesh cases, can be created in the same model object.

- 1 Create a new **mesh** case for **geom1**:

```
mesh1 = model.mesh.create('mesh1', 'geom1');
```



- 2 By default the mesh sequence contains at least a **size** feature, which applies to all the subsequent meshing operations. First create a link to the existing **size** feature and then set the maximum element size **hmax** to **mh** and the minimum element size **hmin** to **mh-mh/3**. Then set the curvature factor **hcurve** to **0.2**:

```
size = mesh1.feature('size');
size.set('hmax', 'mh');
size.set('hmin', 'mh-mh/3');
size.set('hcurve', '0.2');
```

- 3 Create a free tetrahedron mesh:

```
ftet1 = mesh1.feature.create('ftet1', 'FreeTet');
```

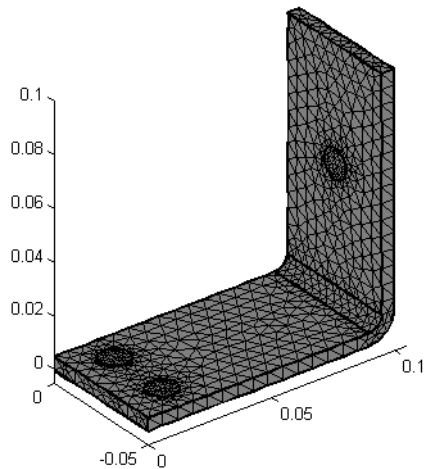
- 4 Build the mesh:

```
mesh1.run;
```

- 5 Visualize the mesh in a MATLAB figure using the command

**mphmesh:**

```
mphmesh(model)
```



## STUDY

---

In order to solve the model you need to create a Study node where the analysis type is set to be solved for:

- 1 Create a **study** node and add a stationary study step:

```
std1 = model.study.create('std1');
stat = std1.feature.create('stat', 'Stationary');
```

- 2 By default the progress bar for the solve and mesh operations is not displayed. To activate the progress bar enter:

```
ModelUtil.showProgress(true)
```

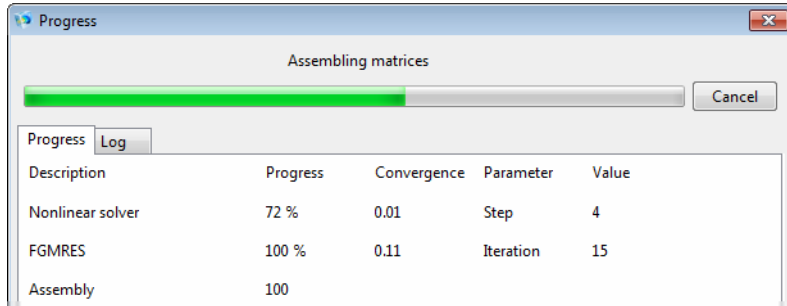
Once activated, the progress bar is displayed in a separate window during mesh or solver operations. The Progress window also contains log information.

**Note:** The progress bar is not available on MAC OS X.

- 3 Solve the model with the command:

```
std1.run;
```

During the computation a window opens to display the progress information and solver log.



**Note:** In this example, no solver related settings were necessary since the study node automatically built the solver sequence based on the study type, physics interface, and the space dimension of the model.

## PLOTTING THE RESULTS

---

Analyze the results by defining plot groups in the results node. To display the generated plots in a MATLAB figure use the `mphpplot` command.

- 1 Create a 3D plot group:

```
pg1 = model.result.create('pg1', 'PlotGroup3D');
```

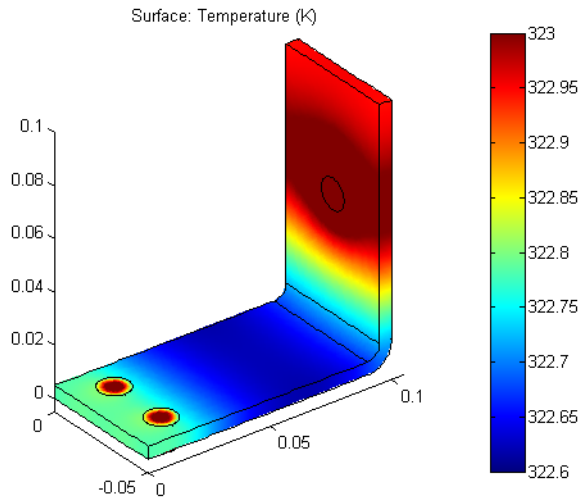
- 2 In the plot group, create a surface plot, activate a manual color range, set the minimum color value to **322.6**, and set the maximum color value to **323**:

```
pg1.feature.create('surf1', 'Surface');
pg1.feature('surf1').set('rangecoloractive', 'on');
pg1.feature('surf1').set('rangecolormin', '322.6');
pg1.feature('surf1').set('rangecolormax', '323');
```

- 3 To display the plot group including a color bar in a MATLAB figure:

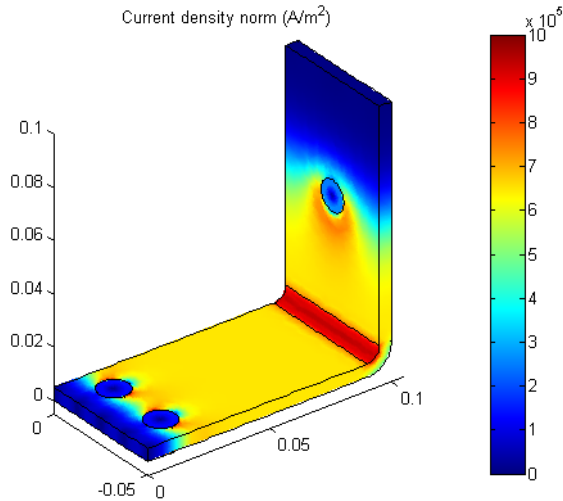
```
mphpplot(model, 'pg1', 'rangenum', 1)
```

If several plot types are available in the same plot group, you can define which color bar to display. The value of the **rangenum** property corresponds to the plot type number in the plot group sequence.



- 4 Create a second plot group, with a surface plot type, and plot the norm of the current density. Set the maximum color range value to **1e6**. Finally, add the title '**Current density norm (A/m<sup>2</sup>)**', display the plot in a MATLAB figure:

```
pg2 = model.result.create('pg2', 'PlotGroup3D');
pg2.feature.create('surf1', 'Surface');
pg2.feature('surf1').set('expr', 'jh.normJ');
pg2.feature('surf1').set('rangecoloractive', 'on');
pg2.feature('surf1').set('rangecolormax', '1e6');
pg2.set('title', 'Current density norm (A/m^2)');
mphplot(model, 'pg2', 'rangenum', 1);
```



## EXPORTING RESULTS

Using the Export node results can be easily exported to a text file.

- By entering the commands below, create a data export node to export the temperature variable  $T$ . Set the filename to `<filepath>\Temperature.txt` where `<filepath>` is replaced with the path to the directory where the file should be saved.

```
data1 = model.result.export.create('data1', 'Data');
data1.setIndex('expr', 'T', 0);
data1.set('filename', 'filepath\Temperature.txt');
data1.run;
```

The above steps extract the temperature at each computational node of the geometry and store the data in a text file in the following format:

```
% Model: busbar.mph
% Version: COMSOL 4.3.0.130
% Date: Apr 30 2012, 11:25
% Dimension: 3
% Nodes: 1787
% Expressions: 1
% Description: Temperature
% x y z T (K)
0.099999999999999999 -0.003838081822546985 0.09639433064874708
322.94988924787606
```

```
0.09749606929798824 -0.006999750297542365 0.1
322.94926137402246
0.09999999999999996 -0.005555555555555556 0.1
322.94824689779085
```

## SAVING THE MODEL

---

1 To save the model using the **save** method enter:

```
model.save('<path>/busbar');
```

In the above command, replace **<path>** with the directory where you would like to save your model. If a path is not defined, the model is saved automatically to the default COMSOL with MATLAB start-up directory. The default start-up directory on Windows and MAC OS X operating systems is usually

**[installdir]\COMSOL43\mli\startup**, where **[installdir]** is the path to the COMSOL installation directory, usually **C:\** on Windows. On a computer running Linux, the start directory is the directory where the command **comsol server matlab** was issued.

The default save format is the COMSOL binary format with the **mph** extension. To save the model as an M-file use the command:

```
model.save('<path>/busbar','m');
```

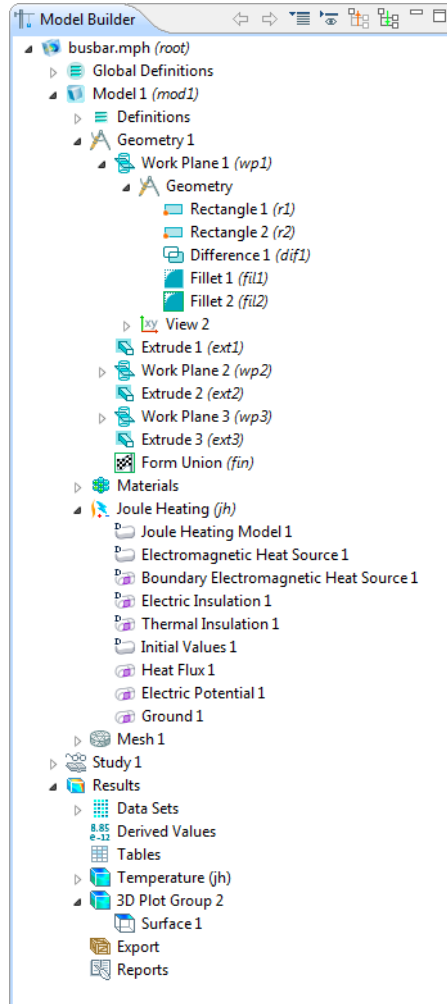
## LOADING THE MODEL TO THE COMSOL DESKTOP

---

Use the COMSOL Desktop to open and examine the model just saved to the **mph** format.

- 1 Start COMSOL Multiphysics stand-alone.
- 2 From the **File** menu select **Open**, then browse to the **mph** file you have just saved and click **Open**.

- 3 By expanding the nodes of the model tree in the **Model Builder** you can examine how the sequence of operations in the model correspond to the commands entered at the MATLAB command line.



## Exchanging Models with the COMSOL Desktop

While building the busbar model in MATLAB you have learned how to save a model as an MPH-file, which then can be opened from the COMSOL Desktop. From the COMSOL Desktop you can also directly transfer models to and from MATLAB.

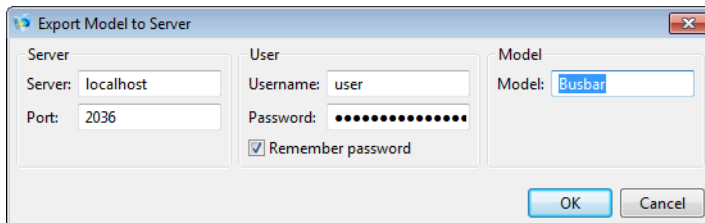
An additional way of transferring a model is in the M-file format. Because this format contains the commands for creating the model, rather than the model itself, you can use it as a starting point to create your own models in MATLAB.

**Note:** On Linux you need to start COMSOL with MATLAB and the COMSOL desktop from the same terminal. Use the ampersand (&) command, for instance, `comsol & or comsol server matlab &`.

### TRANSFERRING A MODEL TO MATLAB

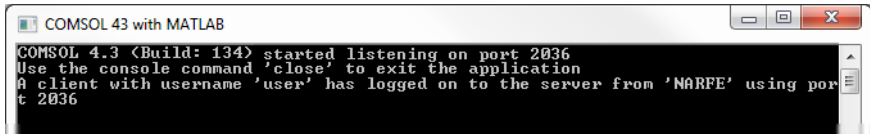
As described in “The COMSOL Client Server”, models created in MATLAB exist on the COMSOL server, which can be either a local or remote server. To transfer a model to MATLAB, export it from the COMSOL Desktop to the COMSOL server and then create a link to the model in the MATLAB workspace.

- 1 If it is not already open, start a new COMSOL Desktop. Choose **View>Model Library**. In the Model Library window, choose **COMSOL Multiphysics>Multiphysics>busbar** and click **Open**.
- 2 Start **COMSOL with MATLAB** (see “Starting COMSOL with MATLAB”).
- 3 In the COMSOL Desktop, go to **File>Client Server>Export Model to Server**.



- 4 Confirm that the correct export information is used:
  - In the **Server** area, define the **Server** name and the **Port** number in the fields. The default server name is `localhost`, which indicates that the COMSOL server is on the same machine. Check the port number by looking at the first line of the text displayed in the COMSOL server window:

COMSOL 4.3 started listening on port 2036



- The **User** area contains the user login information. The **Username** and **Password** fields are set by default based on settings in the user preferences, defined the first time a COMSOL server is started.
- The **Model** area contains the **Model** field where the model object name can be defined to export it from the COMSOL server. For this example enter **Busbar**

**5** Click **OK**.

Now that the model object is stored in the COMSOL server, create a link in MATLAB to gain access to it.

**6** Once the Export model to server window has closed, enter at the MATLAB command line:

```
model = ModelUtil.model('Busbar');
```

Busbar is the model object name, which was defined in step 4 above.

**7** All features of the model can now be accessed, for example, plot the second plot group in a MATLAB figure:

```
mphplot(model, 'pg2', 'rangenum', 1)
```

**8** The model can also be modified, for example, by removing the second plot group from the results node:

```
model.result.remove('pg2');
```

## TRANSFERRING A MODEL TO THE COMSOL DESKTOP

---

As well as transferring your model to MATLAB, the model edited at the MATLAB command line can be transferred to the COMSOL server. It only requires to load the model object from the COMSOL server to the COMSOL Desktop.

**1** Start **COMSOL with MATLAB** and a COMSOL Desktop.

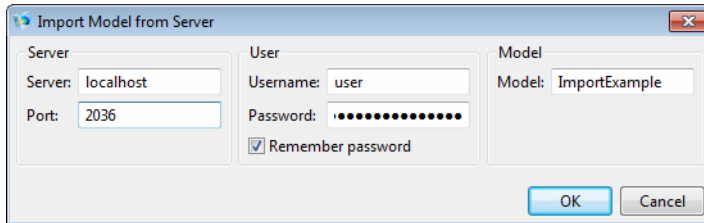
**2** Create a model object, then create a 3D geometry and draw a block:

```
model = ModelUtil.create('ImportExample');
model.geom.create('geom1', 3);
```



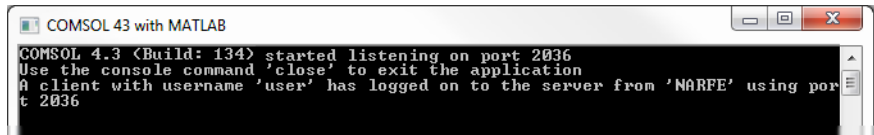
```
model.geom('geom1').feature.create('blk1', 'Block');
model.geom('geom1').run;
```

- 3 In the COMSOL Desktop go to **File>Client Server>Import Model from Server**.



- 4 Make sure the following settings are correct:

- In the **Server** area, define the **Server** name and the **Port** number in the fields. The default server name is `localhost`, which indicates that the COMSOL server is on the same machine. The port number is defined when starting the COMSOL server. The port number is displayed in the COMSOL server window



In the above figure, the port number to use is 2036.

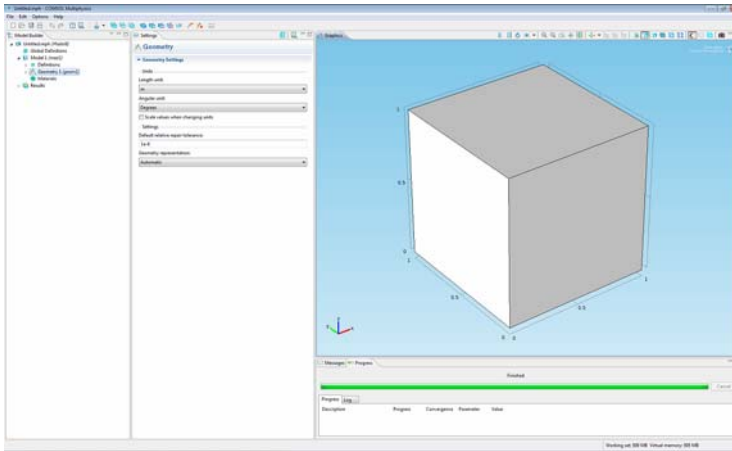
- The **User** area contains the user login information. The **Username** and **Password** fields are set by default based on settings in the user preferences, defined the first time a COMSOL server is started.
- The **Model** area contains the **Model** field where the model object name can be defined to import from the COMSOL server. To get a list of available model objects on the COMSOL server enter at the MATLAB prompt:

```
ModelUtil.tags
```

which for this example returns the following:

```
java.lang.String[]:
 'ImportExample'
```

5 Click **OK**.



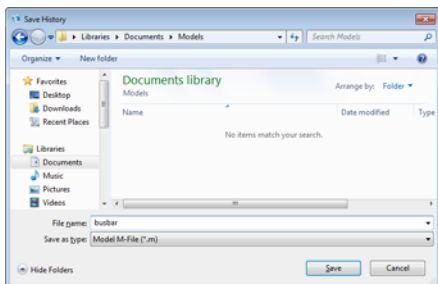
**Note:** It is important to remember that if modifications are made to the model in the COMSOL Desktop, the model needs to be transferred back to MATLAB (the COMSOL server).

## SAVING AND RUNNING A MODEL M-FILE

The easiest way to learn the commands of the COMSOL API is to save a model from the COMSOL Desktop as an M-file. The M-file contains the sequence of commands that create the model. You can open the M-file in a text editor and do modifications to it, as shown in the following example.

**Note:** By default the M-file contains the entire command history of the model, including settings that are no longer part of the model. In order to include only settings that are part of the current model, you need to reset the model history before saving the M-file.

- 1 Start **COMSOL with MATLAB** and a COMSOL Desktop.
- 2 In the COMSOL Desktop go to the **Model Library** page, or select **View>Model Library**.
- 3 In the **Model Library** window, expand the **COMSOL Multiphysics** folder and then the **Multiphysics** folder. Select the **busbar** model and click **Open**.
- 4 In the COMSOL Desktop, choose **File>Reset History**.
- 5 Go to **File>Save As Model M-File**, name it **busbar** and choose the directory to save it to. Click **OK**.



- 6 Open the saved M-file with the MATLAB editor or any text editor and scroll to lines 184–188:

```
model.result('pg3').feature('surf1').set('expr','jh.normJ');
model.result('pg3').feature('surf1').set('rangecolormax','1e6')
```

The commands above define the plot group **pg2**. According to line 184 it includes a surface plot of the expression to **jh.normJ**. On line 188 the maximum color range is set to **1e6**.

- 7 Modify the plot group **pg2** so that it displays the total heat **jh.Qtot** and set the maximum color range to **1e4** instead. Starting on a new line right after line 188, append the following to the M-file:

```
model.result('pg2').feature('surf1').set('expr','jh.Qtot');
model.result('pg2').feature('surf1').set('rangecolormax','1e4');
```

These commands are executed after lines 184–188 and modify plot group **pg2** so that it displays the total heat **jh.Qtot** with a new setting for the maximum value for the color range. Line 184 and 188 can also be modified to achieve the same thing, but this way you can easily revert to the old version.

- 8 Save the modified M-file.
- 9 Run the model at the MATLAB prompt with the command:

```
model = busbar;
```

- 10 Display the plot group **pg2**:

```
mphplot(model,'pg2','rangenum',1)
```

Another way to modify a model object in MATLAB is to export the model from the COMSOL Desktop to MATLAB (see “Transferring a Model to MATLAB”) and then enter the commands in step 5 directly at the MATLAB command line. The benefit of this latter approach is that it does not require running the entire model. See “An Example Using Multiple for Loops”, where this technique is applied.

## Extracting Results at the MATLAB Command Line

LiveLink for MATLAB packages several functions to make it easy to access results directly from the MATLAB command line. These functions are:

- **mpheval**, to evaluate expressions on all node points of a given domain selection,
- **mphinterp**, to evaluate expressions at extracts data arbitrary location,
- **mphglobal**, to evaluate global expressions,
- **mphint**, to integrate value of expressions on selected domains.

Load the model **busbar** from the **Model library** directly at the MATLAB command line.

- 1 Start COMSOL with MATLAB.
- 2 Load the busbar example model from the Model Library. Enter the command:  
`model = mphload('busbar');`

The **mphload** command automatically searches the COMSOL path to find the requested file. You can also specify the path in the file name.

## EVALUATING DATA AT NODE POINTS

---

Use the **mpheval** function to evaluate the electric potential, which is one of the busbar model dependent variables. **mpheval** returns the value of the expression evaluated using the nodes of a simplex mesh. By default the simplex mesh corresponds to the active mesh in the model object.

- 1 Enter at the command line:  
`data = mpheval(model,'V')`

A MATLAB structure is returned according to:

```
data =
 expr: {'V'}
 d1: [1x1787 double]
 p: [3x1787 double]
 t: [4x6416 int32]
 ve: [1787x1 int32]
 unit: {'V'}
```

`mpheval` returns a MATLAB structure defined with the following fields:

- `expr` contains the list of the evaluated expression,
- `d1` contains the data of the evaluated expression,
- `p` contains the coordinates of the evaluation points,
- `t` contains the indices to columns in the `p` field. Each column in the `t` field corresponds to an element of the mesh used for the evaluation,
- `ve` contains the indices of the mesh elements at each evaluation point,
- `unit` contains the unit of the evaluated expression.

- 2 Multiple variables can be evaluated at once, for example both the temperature and the electric potential. Enter:

```
data2 = mpheval(model,{'T' 'V'})
```

This command returns this structure:

```
data2 =
 expr: {'T' 'V'}
 d1: [1x1787 double]
 d2: [1x1787 double]
 p: [3x1787 double]
 t: [4x6416 int32]
 ve: [1787x1 int32]
 unit: {'K' 'V'}
```

The fields `data2.d1` and `data2.d2` contain the values for the temperature and electric potential, respectively.

- 3 Now evaluate the temperature `T` including at the element mid-points as defined by a quadratic shape function. Use the `refine` property and set the property value to 2, which corresponds to the discretization order:

```
data3 = mpheval(model,{'T'},'refine',2)
```

This command returns this structure:

```
data3 =
 expr: {'T'}
 d1: [1x11304 double]
 p: [3x11304 double]
 t: [4x51328 int32]
 ve: [11304x1 int32]
 unit: {'K'}
```

- 4 This step tests how to use the `edim` property in combination with the `selection` property. `edim` allows you to determine the space dimension of the evaluation and `selection` allows you to set the entity number where to evaluate the expression.

Evaluate data on a specific domain, for example the normal current density at boundary number 43:

```
data4 = mpheval(model,{ 'jh.normJ'},...
 'edim',2,'selection',43)
```

This command returns this structure:

```
data4 =
 expr: { 'jh.normJ' }
 d1: [1x36 double]
 p: [3x36 double]
 t: [3x54 int32]
 ve: [36x1 int32]
 unit: { 'A/m^2' }
```

## EVALUATING DATA AT ARBITRARY POINTS

If you want to get data at a specific location not necessarily defined by node points, use the command `mphinterp` to interpolate the results. The interpolation method uses the shape function of the elements.

- 1 To extract the total heat source at `[5e-2;-2e-2;1e-3]` enter:

```
Qtot = mphinterp(model,'jh.Qtot','coord',[5e-2;-2e-2;1e-3])
```

This returns:

```
Qtot =
 7.0214e+003
```

- 2 A grid of points can also be evaluated. Enter the following lines:

```
x0=0:5e-2/4:5e-2;
y0=0:-2.5e-2/4:-2.5e-2;
z0=[0 5e-3];
[x,y,z]=meshgrid(x0,y0,z0);
xx=[x(:),y(:),z(:)]';
Qtot = mphinterp(model,'jh.Qh','coord',xx);
```

- 3 Reshape the variable `Qtot` for a better visualization:

```
Qtot = reshape(Qtot,length(x0),length(y0),length(z0))
```

This results in:

```
Qtot(:,:,1) =
1.0e+005 *
 0.0000 0.0288 0.0742 0.0705 0.0702
 0.0008 0.2894 0.0755 0.0702 0.0702
 0.0000 3.1122 0.0688 0.0699 0.0702
 0.0006 0.2660 0.0731 0.0702 0.0702
 0.0000 0.0281 0.0747 0.0705 0.0702

Qtot(:,:,2) =
1.0e+003 *
```

|        |        |        |        |        |
|--------|--------|--------|--------|--------|
| 0.0012 | 3.0841 | 7.4432 | 7.0454 | 7.0220 |
| 0.0777 | 4.9913 | 7.1107 | 7.0198 | 7.0206 |
| 0.0002 | 8.8581 | 5.5755 | 6.9965 | 7.0198 |
| 0.0606 | 5.0040 | 7.1743 | 7.0202 | 7.0211 |
| 0.0006 | 2.8692 | 7.4441 | 7.0477 | 7.0222 |

## GLOBAL EVALUATION AND INTEGRATION

---

To obtain the maximum value of an expression, create a maximum operator within the COMSOL model object and evaluate its value using the `mphglobal` function.

- 1 Create a maximum operator on domain 1:

```
maxop1 = model.cpl.create('maxop1','Maximum','geom1');
maxop1.selection.set(1);
```

- 2 To access the operator in the results node, update the solution:

```
model.sol('sol1').updateSolution;
```

- 3 To evaluate the global expression defined by `maxop1(T)`:

```
maxT = mphglobal(model,'maxop1(T)')
```

This returns the maximum temperature:

```
maxT =
 323.2986
```

- 4 To calculate the total heat produced in the busbar you can integrate the total heat source, using the command `mphint`. Enter:

```
Q = mphint(model,'jh.Qh','selection',1)
```

The total heat is:

```
Q =
 0.2449
```

- 5 Evaluate the total current passing through boundary 43 and retrieve the unit of the integral:

```
[I unit] = mphint(model,'jh.normJ','edim',2,'selection',43)
I=
 162.2911
unit =
 'A'
```

## Automating with MATLAB Scripts

The LiveLink interface allows you to combine the MATLAB programming tools with the COMSOL model object. A benefit of this integration is to access results at the MATLAB workspace. Another benefit is that you can integrate COMSOL modeling commands into MATLAB scripts, taking full advantage of all available tools for controlling the flow of your code. This section explains how to do this efficiently by introducing MATLAB variables into your COMSOL model and updating only the affected parts of your model object.

### OBTAINING MODEL INFORMATION

---

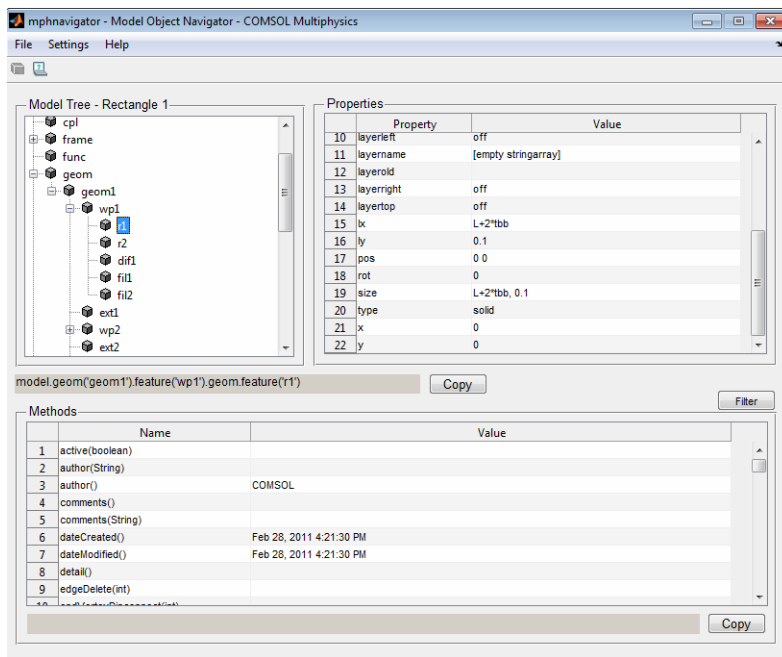
Modifying an existing model object requires you to know how the model is set up. Some functions help you to access this information so that you can add or remove a model feature or modify the value of an existing property. The function `mphnavigator` helps you to retrieve model object information. Calling `mphnavigator` at the MATLAB prompt displays a summary of the features and their properties for the model object available in the MATLAB workspace.

- 1 Start **COMSOL with MATLAB**.
- 1 Load the busbar example model:  

```
model=mphload('busbar');
```
- 2 To access the model information, enter the following command at the MATLAB prompt:  

```
mphnavigator
```





In the mphnavigator graphical user interface the model features are listed under the **Model Tree** section. The nodes can be expanded to access the subfeatures. When selecting a feature from the **Model Tree**, its properties are listed under the **Properties** section. The **Methods** section lists the method available for the selected feature. Just above the **Methods** section, you can see the COMSOL API syntax that lead to the feature. You can copy the command to the clipboard and easily paste it at the MATLAB prompt—just press the **Copy** button to copy the syntax.

- 3 In the **Model Tree**, expand the model feature nodes down to **geom>geom1>wp1>r1** and select the node **r1**.
- 4 In the **Properties** section, you can see that the **lx** property of the geometry feature **r1** is set to  $L+2*tbb$ , this represents the length of the rectangle. The width of the rectangle, represented with the property **ly** is set to 0.1.

## UPDATING MODEL SETTINGS

The COMSOL model object allows you to modify parameters, features, or feature properties, using the `set` method. Once a property value is updated, you can run the appropriate sequence, depending on where the changes were introduced into the model—for example, the geometry or the mesh sequence. Running the solver sequence automatically runs all sequences where modified settings are detected.

Starting with the busbar model described in “A Thorough Example: The Busbar”, this section modifies a parameter value and re-solves the model. For this purpose, the geometry of the model is prepared using parameters such as `L`, the length of the busbar, and `tbb`, the thickness of the busbar.

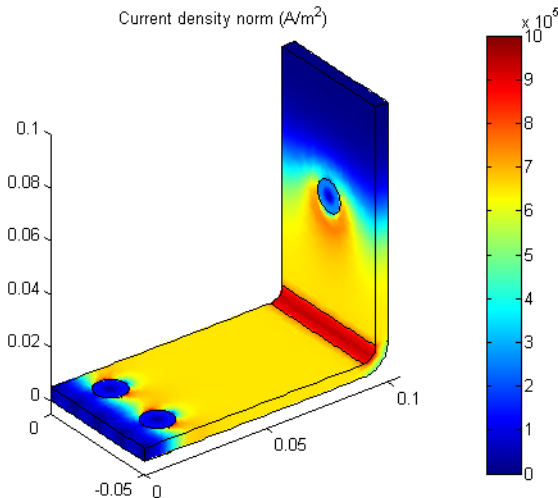
1 Start **COMSOL with MATLAB** (if you have not done so already).

2 Load the model from the COMSOL model library:

```
model = mphload('busbar');
```

3 Plot the current solution with this command:

```
mphplot(model, 'pg2', 'rangenorm', 1);
```



4 The first exercise changes the length of the parameters `L` (length of the busbar). Enter:

```
model.param.set('L', '18[cm]');
```

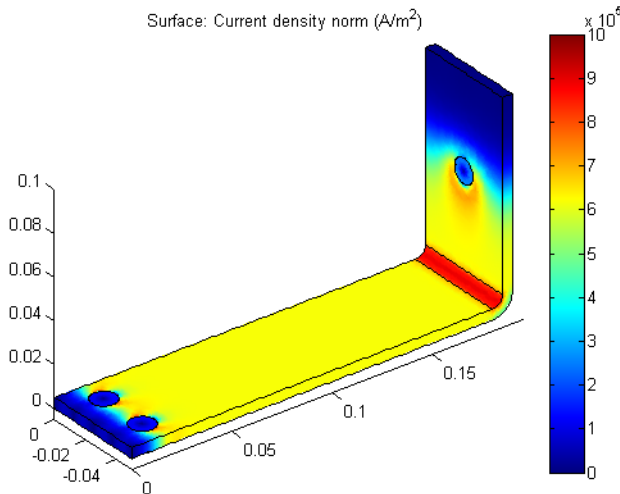
5 To run the solver sequence and compute the solution enter:

```
model.sol('sol1').run;
```

**Note:** The solver node automatically detects all modifications in the model, and runs the geometry or mesh sequences when needed. Here, the new value for the parameter **L** induces a change in the geometry and thus a new mesh is also needed. Full associativity is also ensured making sure that all physics settings remain applied as in the original model.

- 6 Plot the updated solution, which results in the geometry change:

```
mphplot(model, 'pg2', 'rangenum', 1);
```



## USING MATLAB VARIABLES IN THE COMSOL MODEL

Use the **set** method described in the previous section to define the feature properties using MATLAB variables. It is important to make sure that the value of the MATLAB variable is consistent with the units used in the model. Before beginning, make sure that the busbar model used in the previous section is loaded into MATLAB.

First, change the length of the busbar, described by the parameter **L**.

- 1 Create a MATLAB variable **L0** equal to **9e-2**:

```
L0 = 9e-2;
```

- 2 Update the value of the parameter **L** with the variable **L0**:

```
model.param.set('L', L0);
```

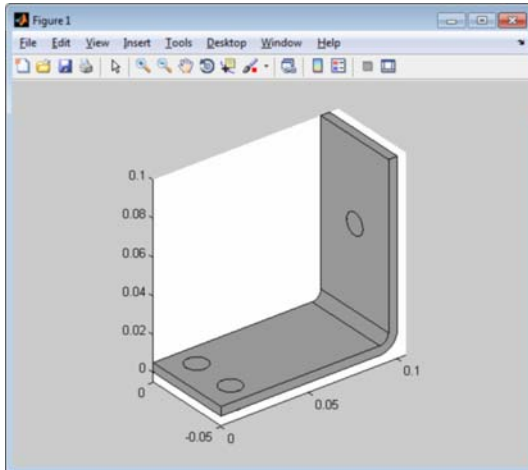
**Note:** In contrast to this command, setting a value using an expression from within the model object requires the second argument to be a string expression, as shown in “Updating Model Settings”.

3 Re-run the geometry sequence to update the geometry:

```
model.geom('geom1').run;
```

4 To display the new geometry enter:

```
mphgeom(model,'geom1')
```



Working with parameters is convenient, since there is one place where you need to go to view or modify the current configuration of the model. The next step uses a different method, where a feature node is edited to modify its properties. For example, to modify the busbar geometry, the rectangles **r1** and **r2** generated in the work plane **wp1** are edited.

5 Start to create links to the geometry feature **r1** and **r2** by entering the commands:

```
r1 = model.geom('geom1').feature('wp1').geom.feature('r1');
r2 = model.geom('geom1').feature('wp1').geom.feature('r2');
```

6 Enter the following command to define MATLAB variables:

```
H1 = 0.2;
H2 = 0.195;
```

7 Set the height of rectangles **r1** and **r2** using the variables **H1** and **H2**, respectively.

```
r1.set('ly', H1);
r2.set('ly', H2);
```

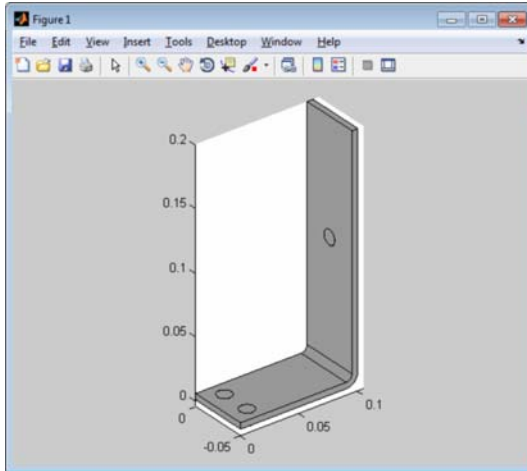
**Note:** The function **mphproperties** can be used to get a list of properties and values for feature nodes of a model. See “Obtaining Model Information” for more details.

8 To update the geometry, enter:

```
model.geom('geom1').run;
```

9 Enter this command to plot the geometry:

```
mphgeom(model,'geom1');
```



There is a third option when defining property values for features: to combine MATLAB variables with parameters or variables defined within the COMSOL model object. To do this the MATLAB variable just needs to be converted to a string.

This last exercise tests this by changing the height of rectangle **r1** and **r2** to **L0**, and **L0-tbb**, respectively, where **L0** is a MATLAB variable.

10 Define the variable **L0**:

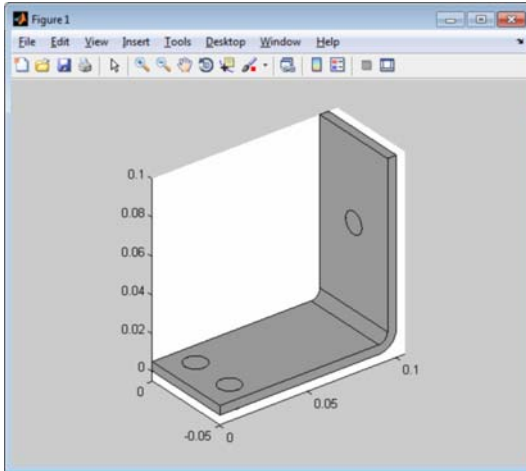
```
L0 = 0.1;
```

11 Modify the **ly** property of rectangles **r1** and **r2**:

```
r1.set('ly',L0)
r2.set('ly',[num2str(L0) ' -tbb']);
```

12 Update and plot the geometry:

```
model.geom('geom1').run;
mphgeom(model,'geom1');
```



## AN EXAMPLE USING MULTIPLE FOR LOOPS

---

In this example, a MATLAB function is created that solves the busbar model for different values of the length and thickness of the busbar, and the input electric potential. The function evaluates and returns the maximum temperature in the busbar; the generated heat, and the current through the busbar. For each variation of the model the function stores these results in a file and saves the model object in a MPH file. To make it easy to identify the name of the MPH-file, it contains the values of the different parameters used to set-up the model.

The input argument of the M-function is the busbar model object and the path to the directory where the data and models are saved.

- 1 Open a text editor, for example the MATLAB text editor.
- 2 At the first line of a new M-file, enter the following function header:

```
function modelParam(model,filepath)
```

The function first creates a file and then sets the header of the output file format.

- 3 In the text editor continue to enter the following lines:

```
filename = fullfile(filepath,'results.txt');
fid=fopen(filename,'wt');
fprintf(fid,'*** run parametric study ***\n');
fprintf(fid,'L[m] | tbb[m] | Vtot[V] | ');
fprintf(fid,'MaxT[K] | TotQ[W] | Current[A]\n');
```

- 4 In order to evaluate the maximum values add a coupling operator to the model. Enter the lines:

```
maxop1 = model.cpl.create('maxop1','Maximum','geom1');
maxop1.selection.set(1);
```

- 5 When running a large amount of iteration, the model history can be disabled to prevent the memory from rising along the iterations due to the model history stored in the model. Enter the lines:

```
model.hist.disable;
```

- 6 Now start a **for** loop to parameterize the parameter **L** and set the corresponding parameter in the model object. Enter the commands:

```
for L = [9e-2 15e-2]
model.param.set('L',L);
```

- 7 Continue by creating a second **for** loop, this time to parameterize the parameter **tbb** and to modify its value in the model object:

```
for tbb = [5e-3 10e-3]
model.param.set('tbb',tbb);
```

- 8 Define the last **for** loop to parameterize the applied potential **Vtot**:

```
for Vtot = [20e-3 40e-3]
model.param.set('Vtot',Vtot);
```

- 9 For each version of the model write the parameter values to the output file:

```
fprintf(fid,[num2str(L),' | ',num2str(tbb),...
' | ',num2str(Vtot),' | ']);
```

- 10 To solve the model, add the line below:

```
model.sol('sol1').run;
```

- 11 The following lines evaluate the results:

```
MaxT = mphglobal(model,'maxop1(T)');
TotQ = mphint(model,'jh.Qtot','selection',1);
Current = mphint(model,'jh.normJ',...
'edim',2,'selection',43);
```

- 12 Save the results to the output text file:

```
fprintf(fid,[num2str(MaxT),' | ',num2str(TotQ),...
' | ',num2str(Current),' \n']);
```

**I3** Name and save the model:

```
modelName = fullfile(filepath,['busbar_L=',num2str(L),...
'_tbb=',num2str(tbb),...
'_Vtot=',num2str(Vtot),'.mph']);
model.save(modelName);
```

**I4** Terminate the for loops:

```
end
end
end
```

**I5** Close the output text file:

```
fclose(fid);
```

The script in the text editor should now look like this text:

```
function modelParam(model,filepath)
filename = fullfile(filepath,'results.txt');
fid=fopen(filename,'wt');
fprintf(fid,'*** run parametric study ***\n');
fprintf(fid,'L[m] | tbb[m] | Vtot[V] | ');
fprintf(fid,'MaxT[K] | TotQ[W] | Current[A]\n');
maxop1 = model.cpl.create('maxop1','Maximum','geom1');
maxop1.selection.set(1);
model.hist.disable;
for L = [9e-2 15e-2]
 model.param.set('L',L);
 for tbb = [5e-3 10e-3]
 model.param.set('tbb',tbb);
 for Vtot = [20e-3 40e-3]
 model.param.set('Vtot',Vtot);
 fprintf(fid,[num2str(L),' | ',num2str(tbb),...
 ' | ',num2str(Vtot),'\n']);
 model.sol('sol1').run;
 MaxT = mphglobal(model,'maxop1(T)');
 TotQ = mphint(model,'jh.Qtot','selection',1);
 Current = mphint(model,'jh.normJ',...
 'edim',2,'selection',43);
 fprintf(fid,[num2str(MaxT),' | ',num2str(TotQ),...
 ' | ',num2str(Current),'\n']);
 modelName = fullfile(filepath,['busbar_L=',num2str(L),...
 '_tbb=',num2str(tbb),...
 '_Vtot=',num2str(Vtot),'.mph']);
 model.save(modelName);
 end
 end
end
fclose(fid);
```

**I6** Save the M-file as `modelParam.m` in a directory known by MATLAB.



**17** If **COMSOL with MATLAB** is not already running, start it now and load the model busbar from the Model library:

```
model = mphload('busbar');
```

**18** Run the function, substitute 'filepath' to a directory of your choice:

```
modelParam(model, 'filepath')
```

**19** Open the file **results.txt** in a text editor to look at the summary of the results:

```
*** run parametric study ***
L[m] | tbb[m] | Vtot[V] | MaxT[K] | TotQ[W] | Current[A]
0.09 | 0.005 | 0.02 | 323.2995 | 0.24501 | 162.3327
0.09 | 0.005 | 0.04 | 413.7479 | 0.98005 | 324.6654
0.09 | 0.01 | 0.02 | 308.6479 | 0.047819 | 96.3541
0.09 | 0.01 | 0.04 | 355.1416 | 0.19127 | 192.7082
0.15 | 0.005 | 0.02 | 315.883 | 0.32864 | 157.2614
0.15 | 0.005 | 0.04 | 384.0821 | 1.3146 | 314.5229
0.15 | 0.01 | 0.02 | 305.1893 | 0.065051 | 95.3758
0.15 | 0.01 | 0.04 | 341.3074 | 0.2602 | 190.7516
```

Although this example duplicates functionality that is readily accessible in the COMSOL Desktop, you can, by using a similar technique, couple a COMSOL model to your customized optimization script.

## Using External MATLAB Functions

Another advantage of using LiveLink for MATLAB is the ability to call a MATLAB function directly from within the COMSOL Desktop. You can use the function to define, within the COMSOL model object, properties such as material definitions or physics settings. COMSOL automatically detects the external function and starts the MATLAB engine to evaluate it. The function output is then applied to the corresponding property.

To use this functionality, just start the COMSOL Desktop and MATLAB automatically starts in the background when needed.

**Note:** On Linux operating systems, specify the MATLAB root directory path `MLROOT` and load the `gcc` library when starting the COMSOL Desktop: `comsol -mlroot MLROOT -forcegcc`.

The example in this section illustrates how to use external MATLAB functions in a COMSOL model. The model computes for the temperature distribution in a material subjected to an external heat flux. Both the thermal conductivity of the material and the applied heat flux are defined by MATLAB functions.

### CREATING THE MATLAB FUNCTIONS

---

Assume that the material in the example is characterized by a random thermal conductivity. To define the thermal conductivity, create a MATLAB function with the location along the x-axis as an input argument and let the conductivity vary randomly within 200 W/(m\*K) around a constant value of 400 W/(m\*K).

Define a second MATLAB function for the external heat flux to be a function of the following arguments:

- `x` and `y`, the location coordinates.
- `x0` and `y0`, the coordinates of the center of application of the heat source.
- `Q0`, the maximum heat source.
- `scale`, a parameter that scale the period of the heat flux.

`x` and `y` are dependent variables of the model. `x0`, `y0`, `Q0`, and `scale` are defined with constant value in this exercise.

1 Open a text editor, for example the MATLAB text editor.

2 In a new file enter:

```
function out=conductivity(x)
out = 400+5*randn(size(x));
```

3 Save the file as **conductivity.m**.

4 Create a new file and enter:

```
function out = heatflux(x,y,x0,y0,Q0,scale)
radius = sqrt((x-x0).^2+(y-y0).^2);
out = Q0/5+Q0/2.*sin(scale*pi.*radius)./(scale*pi.*radius);
```

5 Save the file as **HeatFlux.m**.

**Note:** For both functions the input arguments have the size of the space coordinate variables **x** and **y**. These variables are defined as arrays, and the function needs to return an array with the same size as the input arguments. Ensure that this is the case by using the **size** command and pointwise operators (**.\*** and **./**).

## MODEL WIZARD

---

1 Start COMSOL Multiphysics.

2 In the **Model Wizard** window, on the **Select Space Dimension** page, select **3D**. Click **Next** ➡.

3 On the **Add Physics** page, select **Heat Transfer > Heat Transfer in Solids(ht)**. Click **Next** ➡.

4 On the **Select Study Type** page, under **Preset Studies** select **Stationary** 📄.

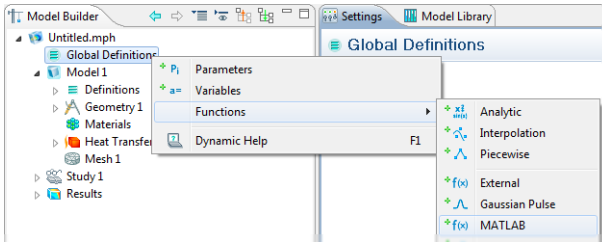
5 Click **Finish** 🏁.

## DEFINING THE EXTERNAL MATLAB FUNCTIONS IN THE MODEL

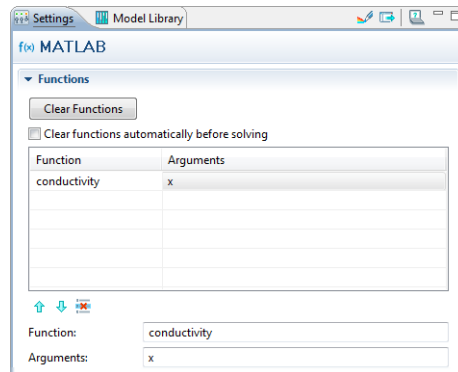
---

You have noticed that the two MATLAB functions are highlighted in orange after being entered. This is because they need to be defined in the model before COMSOL can recognize them as external MATLAB functions.

- 1 Right-click **Global Definitions** node and select **Functions > MATLAB**.



- 2 On the **Settings** page, under the **Functions** section in the **Function** field enter **conductivity** and under the **Arguments** field enter **x**.



By defining the function here, COMSOL knows that conductivity is a MATLAB function. COMSOL automatically starts MATLAB to evaluate the function when necessary.

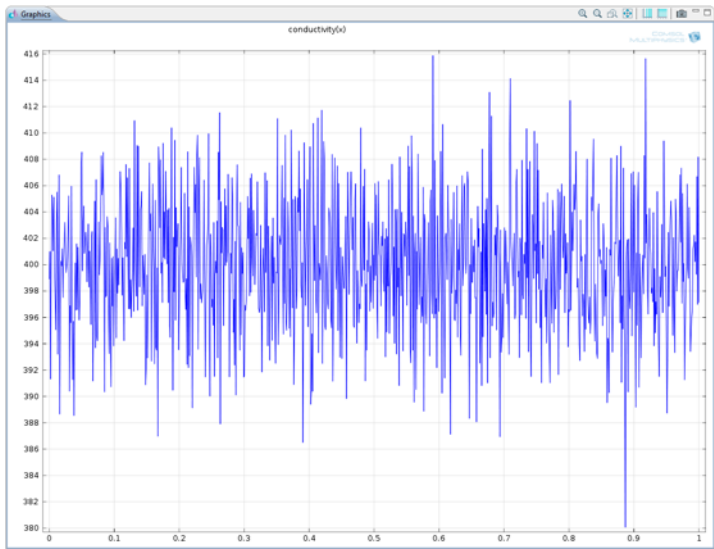
**Note:** Saving the COMSOL model at the location (as for the external MATLAB functions) ensures that the functions path is known by MATLAB. Other alternatives consist in setting the function path directly in MATLAB before running the model or setting the environment variable COMSOL\_MATLAB\_PATH with the directory path of the functions.

- 3 Go to the **File** menu, select **Save As**, and browse to the directory where the files **conductivity.m** and **heatflux.m** are stored.

You can display the value of the function defined by first defining the plot limit for the input arguments.

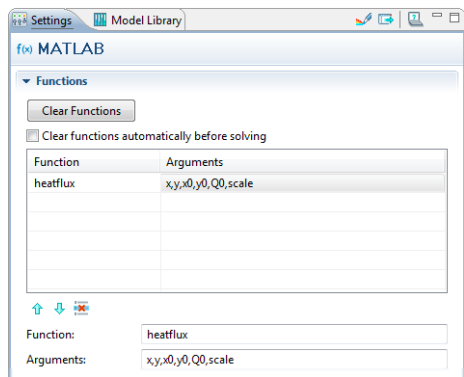
- 4 Expand the **Plot parameters** section. In the associated table enter **0** as **Lower limit** and **1** as **Upper limit**.

5 Click the **Plot** button .



You can now define a second MATLAB function that returns the heat flux condition.

6 Repeating the above procedure, add a new MATLAB function. On the **Settings** page under **Functions** section, enter **heatflux** in the **Function** field and set the **Arguments** field with **x,y,x0,y0,Q0,scale**.

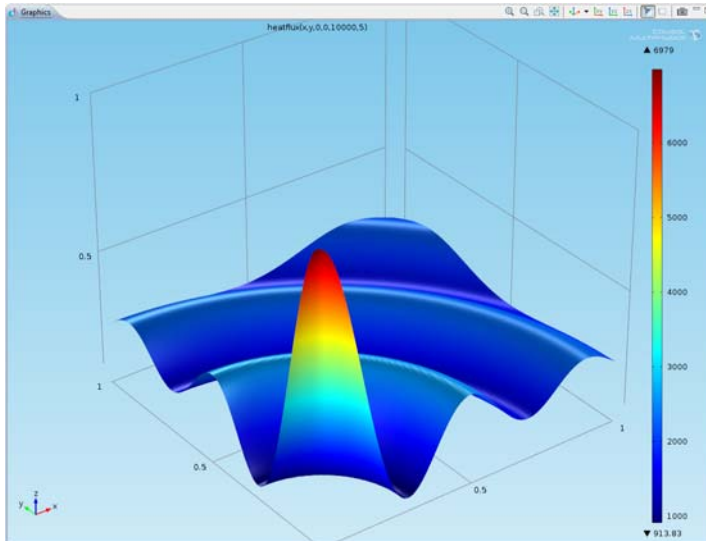


7 To display the function enter the following in the **Plot parameters** table:


| LOWER LIMIT | UPPER LIMIT |
|-------------|-------------|
| 0           | 1           |
| 0           | 1           |
| 0           | 0           |
| 0           | 0           |

|             |             |
|-------------|-------------|
| LOWER LIMIT | UPPER LIMIT |
| 1e4         | 1e4         |
| 5           | 5           |

8 Click the **Plot** button .



## GEOMETRY AND MATERIAL DEFINITION

1 Right-click the **Geometry 1** node and select **Block** .

2 Click **Build All**.

3 Right-click the **Materials** node and select **Material**.


4 Under **Material Contents**, in the **Value** column set the expression of the **Thermal conductivity** to `conductivity(x)`, the expression of **Density** to `8e3` and the expression of **Heat Capacity at Constant Pressure** to `2e3`.

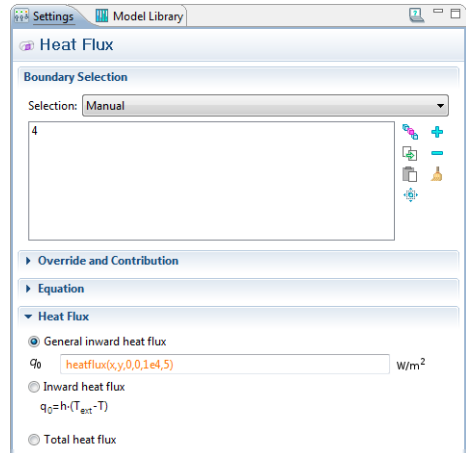
| Material Contents                    |      |                 |          |
|--------------------------------------|------|-----------------|----------|
| Property                             | Name | Value           | Unit     |
| ✓ Thermal conductivity               | k    | conductivity(x) | W/(m*K)  |
| ✓ Density                            | rho  | 8e3             | kg/m^3   |
| ✓ Heat capacity at constant pressure | Cp   | 2e3             | J/(kg*K) |

**Note:** The expression `conductivity(x)` displays in orange as the MATLAB function is unitless.

## HEAT TRANSFER IN SOLIDS

---



- 1 Add a constant temperature boundary condition. Right-click **Heat Transfer in Solids**, then select **Temperature**.
- 2 On the **Temperature** settings page, select boundaries **3**, **5**, and **6** (You can also use the **Paste Selection** button  to enter directly the selection).
- 3 To add a boundary heat flux right-click **Heat Transfer in Solids** node, and select **Heat Flux**.
- 4 On the **Heat flux** settings page select boundary **4** and set the **General inward heat flux** expression to `heatflux(x,y,0.5,0.5,1e4,3)`.

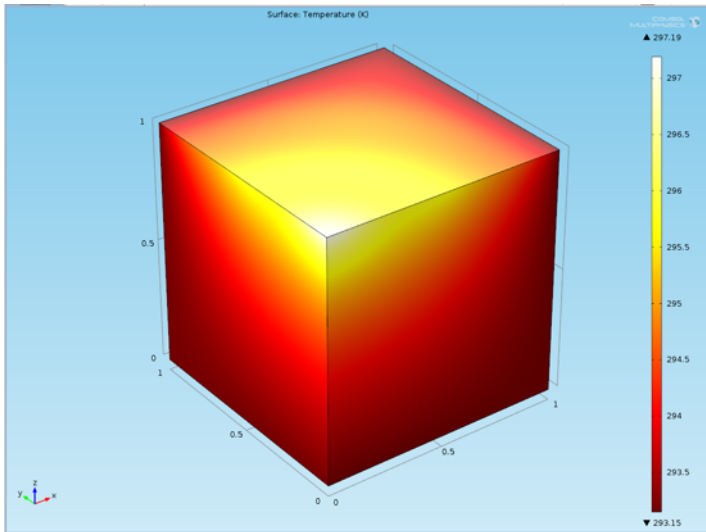


## COMPUTING AND PLOTTING THE RESULTS

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Once the model is set-up the solution can be computed. A default mesh is automatically generated.

- 1 Right-click the **Study** node  and select **Compute** .
- 2 Click the **Temperature (ht)** node to display the temperature field at the geometry surface.



- 3 Visualize the material thermal conductivity in the geometry by adding a new 3D Plot group in the **Results** node. Then right-click **3D Plot group 3** node and select **Isosurface**.
- 4 On the associated **Settings** page, under the **Expression** section, enter `conductivity(x)` in the **Expression** field.
- 5 Under **Levels** section change the **Total levels** to 15.
- 6 Click the **Plot** button.

